

BRONX COMMUNITY COLLEGE
of the City University of New York

DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE

MATH 30
Nikos Apostolakis

Midterm
March 25, 2010

Name: _____

Directions: Write your answers in the provided space. To get full credit you *must* show all your work. Simplify your answers whenever possible. Be certain to indicate your final answer clearly. This exam has a total of 100 points.

1. Find the domain for each of the following functions:

(a) (10 points) $f(x) = \frac{2x - 1}{x^2 - x - 12}$

(b) (10 points) $g(x) = \sqrt{x^2 - 4}$

(c) (10 points) $h(x) = \log_2(9 - x^2)$

2. (10 points) Find $f \circ g$, where $f(x) = \frac{2x - 3}{5x + 2}$ and $g(x) = \frac{x - 1}{x + 2}$

3. (10 points) Let $f(x) = x^2 - 4x - 2$ with domain $[-\infty, 2)$, and $g(x) = 2 - \sqrt{x + 6}$. Prove that f and g are a pair of inverse functions.

4. (10 points) Find the formula, the domain and the range of f^{-1} , where

$$f(x) = \frac{-x + 3}{4x - 7}$$

5. (5 points) List all possible rational roots of the following polynomial, according to the “Rational Root Theorem”.

$$p(x) = 6x^5 - 3x^4 + 7x^3 - 2x^2 + 8x - 12$$

6. (15 points) Solve the following equation:

$$x^5 - 5x^4 - x^3 + 11x^2 - 6 = 0$$

7. (20 points) Solve the following inequality:

$$x^4 - 4x^3 + 3x^2 + 4x - 4 \geq 0$$