Quiz $2\frac{1}{2}$ for CSI35

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Directions: This quiz is due Thursday October 2, at 2:00 PM.

- 1. Recall that a *bit string* is a word on the alphabet $\{0, 1\}$. Let *I* be the function that counts the number of ones in a bit string *s*.
 - (a) Give a recursive definition of I(s).
 - (b) Use structural induction to prove that for two string bits s and t we have:

$$I(st) = I(s) + I(t)$$

where, st stands for the concatenation of the two strings s and t.

(c) Let O(s) be the function that counts the number of zeros in s (this was defined in the previous homework), and let l(s) be the length of s. Prove that:

$$l(s) = O(s) + I(s)$$

for all bitstrings s.