# Mathematics 13 Fall 2005 <br> Instructor : Nikolaos Apostolakis <br> Second Exam (Take Home) <br> November 292005 

This exam is due Monday December 5, at 2:00 pm. Answer all questions. In order to get full credit you should fully justify your answers. Please present a neat and organized document.

1. Find the domain of the function: $\quad f(x)=\ln (\ln (3 x-2))$.
2. Express as a sum difference or multiple of logarithms: $\log \left(\frac{(x-y) \sqrt[3]{(x+5)^{2}}}{x^{3} y^{2}}\right)$.
3. Solve for $y: \quad \log y^{5}-2 \log \left(x^{3}+2 x^{2}-5\right)+3 \log (x+4)=1$.
4. Solve: $2^{x+1}=3^{x}$.
5. Solve: $\quad 3^{x}-15 \cdot\left(3^{-x}\right)=-2$.
6. Sketch a graph of the function: $y=\sec x$.
7. Sketch a graph of the function: $\quad y=4 \sin \left(3 x+\frac{\pi}{4}\right)$.
8. Prove: $\csc \theta \sec \theta-\cot \theta=\tan \theta$.
9. Solve: $\sin 2 x-\sin 4 x=0$.
10. Let $\theta$ be an angle with $0<\theta \leq \pi$. Find $\cos \theta$ if $\cot \theta=3$.
11. Find: $\sin \left(\tan ^{-1} x\right)$.
